CubeHash efficiency estimates (2.B.2)

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This document is a statement of CubeHash’s estimated computational efficiency and memory requirements in hardware and software across a variety of platforms.

General comments. CubeHashr/b xors a b-byte input block to the first b bytes of its 1024-bit state, applies an invertible transformation consisting of r identical rounds, and then moves on to the next input block. Consequently CubeHashr/b uses r rounds for each b-byte block; the time taken by CubeHashr/b is approximately linear in r/b.

CubeHashr/b–h has an initial overhead of 10r rounds to build an initial state given the round count r, the block size b, and the output length h. This overhead can be trivially eliminated at the expense of 128 bytes of constant storage for each desired (r, b, h).

CubeHashr/b–h also has a final overhead of 10r rounds, approximately the cost of hashing an additional 10b bytes. For comparison, SHA–256 uses between 8 and 72 bytes of padding, and SHA–512 uses between 16 and 144 bytes of padding.


Estimates were generated from the following calculation: The Core 2 Duo can perform three simple 128-bit vector operations in each cycle. Adding one vector of four 32-bit words to another is a single vector operation, so the 32 word additions in a CubeHash round are eight vector operations, estimated to take 8/3 cycles. Similar comments apply to xor. The 32 word rotations can be implemented as eight copies, sixteen shifts, and eight xors, estimated to take 32/3 cycles. An additional 8/3 cycles are required for eight vector permutations. Together with loop overhead each round is therefore estimated to take 20 cycles.

Estimated clock cycles for a 512-bit message digest: 200r cycles to compute the initial state; 20r cycles for each b-byte message block; 200r cycles to compute the digest. In other words: 20r/b cycles per byte, with an overhead of 20b bytes.

Estimated clock cycles for a 384-bit message digest: Same.

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Estimated clock cycles for a 256-bit message digest: Same.
Estimated clock cycles for a 224-bit message digest: Same.

Time-memory tradeoffs: The initial state can be precomputed, as discussed above, eliminating 10\(b\) bytes of overhead.


Estimates were generated from the following calculation: See above for a description of the Core 2 Duo’s vector capabilities. Only 8 128-bit vector registers are available in 32-bit mode; this might seem to be enough for CubeHash, but rotation uses an extra register, so some extra loads and stores are required. Each round is therefore estimated to take 25 cycles.

Estimated clock cycles for a 512-bit message digest: 250\(r\) cycles to compute the initial state; 25\(r\) cycles for each \(b\)-byte message block; 250\(r\) cycles to compute the digest. In other words, 25\(r/b\) cycles per byte, with an overhead of 20\(b\) bytes.

Estimated clock cycles for a 384-bit message digest: Same.
Estimated clock cycles for a 256-bit message digest: Same.
Estimated clock cycles for a 224-bit message digest: Same.

Time-memory tradeoffs: The initial state can be precomputed, as discussed above, eliminating 10\(b\) bytes of overhead.

Efficiency estimates for 8-bit processors. Description of platform used to generate the estimates: Atmel ATmega8, 16MHz clock speed, 1024 bytes of static RAM.

Estimates were generated from the following calculation: An ATmega8 round is estimated to take approximately 2000 cycles per round. This estimate was derived from the following comparison to the Core 2 Duo: a Core 2 Duo cycle performs 12 32-bit operations, typically equivalent to 48 8-bit operations, each of which takes 1 cycle on the ATmega8; loads and stores are estimated to cost an extra factor of approximately 2. Note that the CubeHash state fits comfortably into the static RAM on the ATmega8, and that the hypercube structure in CubeHash permits some locality of reference.

Estimated clock cycles for a 512-bit message digest: 20000\(r\) cycles to compute the initial state; 2000\(r\) cycles for each \(b\)-byte message block; 20000\(r\) cycles to compute the digest. In other words: 2000\(r/b\) cycles per byte, with an overhead of 20\(b\) bytes.

Estimated clock cycles for a 384-bit message digest: Same.
Estimated clock cycles for a 256-bit message digest: Same.
Estimated clock cycles for a 224-bit message digest: Same.

Time-memory tradeoffs: The initial state can be precomputed, as discussed above, eliminating 10\(b\) bytes of overhead.

Efficiency estimates for ASICs. Description of platform used to generate the estimates: ASIC built with a standard 130nm process.
Estimates were generated from calculations shown below.

Estimated gate count: A fully unrolled, purely combinatorial round uses 1024 full adders (each 10 gate equivalents) and 1024 xors (each 4 gate equivalents), plus 1024 D-type flip-flops (each 8 gate equivalents) to store the resulting state, for a total of approximately 23000 gate equivalents. There are several ways that this area can be improved without sacrificing speed, for example using the Ling adder. (On the other hand, to improve clock speed one might also consider using more gates to reduce adder latency.) The benefit of full unrolling is that each round takes just one clock cycle.

Estimated clock cycles for a 512-bit message digest: 10r cycles to compute the initial state; r cycles for each b-byte message block; 10r cycles to compute the digest. In other words: r/b cycles per byte, with an overhead of 20b bytes.

Estimated clock cycles for a 384-bit message digest: Same.
Estimated clock cycles for a 256-bit message digest: Same.
Estimated clock cycles for a 224-bit message digest: Same.

Time-memory tradeoffs: The parallelism and regular structure of CubeHash allows a wide variety of choices for the hardware implementor.